

## UNIVARIATE CASE

TERMINOLOGY	NOTATION	RELATED FORMULAS
RANDOM VARIABLE	X, Y, Z, etc.	
PARTICULAR VALUE OF A RANDOM VARIABLE	a, b, i, j, n, x, y, z, w etc.	
CUMULATIVE DISTRIBUTION FUNCTION (cdf) OR DISTRIBUTION FUNCTION (df)	F(.)	$F(b) = P(X \leq b)$ $P\{a < X \leq b\} = F(b) - F(a)$  FOR DISCRETE CASE  $F(a) = \sum_{\text{all } x_i \leq a} p(x_i)$  FOR CONTINUOUS CASE $F(a) = \int_{-\infty}^a f(x) dx$
PROBABILITY MASS FUNCTION (pmf) (discrete case)	p(.)	$p(a) = P(X=a)$
PROBABILITY DENSITY FUNCTION (pdf) (continuous case)	f(.)	$f(a) = \frac{d}{da} F(a)$ $P(X=a) = 0$ $P(X \in B) = \int_B f(x) dx$ $P\{a \leq X \leq b\} = \int_a^b f(x) dx$
EXPECTATION OF A RANDOM VARIABLE (EXPECTED VALUE OF X)	E[X]	FOR DISCRETE CASE $E[X] = \sum_{x:p(x)>0} xp(x)$  FOR CONTINUOUS CASE $E[X] = \int_{-\infty}^{\infty} xf(x) dx$
EXPECTATION OF A FUNCTION OF A RANDOM VARIABLE (g(X))	E[g(X)]	FOR DISCRETE CASE $E[g(X)] = \sum_{x:p(x)>0} g(x)p(x)$ FOR CONTINUOUS CASE $E[g(X)] = \int_{-\infty}^{\infty} g(x)f(x) dx$ IN GENERAL $E[aX + b] = aE[X] + b$
nth MOMENT OF A RANDOM VARIABLE	E[X <sup>n</sup> ]	FOR DISCRETE CASE $E[X^n] = \sum_{x:p(x)>0} x^n p(x)$ FOR CONTINUOUS CASE $E[X^n] = \int_{-\infty}^{\infty} x^n f(x) dx$
VARIANCE OF A RANDOM VARIABLE	Var(X)	$Var(X) = E[(X - E[X])^2] = E[X^2] - (E[X])^2$ $Var(aX + b) = a^2 Var(X)$
MOMENT GENERATING FUNCTION OF A RANDOM VARIABLE	$\phi(t)$ or $\phi_X(t)$	IN GENERAL $\phi(t) = E[e^{tX}]$ FOR DISCRETE CASE  $\phi(t) = \sum_{x:p(x)>0} e^{tx} p(x)$ FOR CONTINUOUS CASE  $\phi(t) = \int_{-\infty}^{\infty} e^{tx} f(x) dx$ IN GENERAL $\phi'(0) = E[X]$ $\phi^n(0) = E[X^n], n \geq 1$

**MULTIVARIATE CASE  
(JOINTLY DISTRIBUTED RANDOM VARIABLES)**

TERMINOLOGY	NOTATION	RELATED FORMULAS
JOINT CUMULATIVE PROBABILITY DISTRIBUTION FUNCTION (jcdf or jdf) OF X AND Y	$F(\cdot, \cdot)$	$F(a, b) = P\{X \leq a, Y \leq b\}$
MARGINAL DISTRIBUTION FUNCTION OF X (Y)	$F_X(\cdot)$ ( $F_Y(\cdot)$ )	$F_X(a) = F(a, \infty) = P\{X \leq a\}$ $(F_Y(b) = F(\infty, b) = P\{Y \leq b\})$
JOINT PROBABILITY MASS FUNCTION OF X AND Y (jpmf) (discrete case)	$p(\cdot, \cdot)$	$p(x, y) = P\{X=x, Y=y\}$ $p_X(x) = \sum_{y: p(x, y) > 0} p(x, y)$ $p_Y(y) = \sum_{x: p(x, y) > 0} p(x, y)$
JOINT PROBABILITY DENSITY FUNCTION OF X AND Y (jpdf) (continuous case)	$f(\cdot, \cdot)$	$P(X \in A, Y \in B) = \int_B \int_A f(x, y) dx dy$ $f_X(x) = \int_{-\infty}^{\infty} f(x, y) dy$ $f_Y(y) = \int_{-\infty}^{\infty} f(x, y) dx$
EXPECTATION OF FUNCTIONS OF TWO VARIABLES X AND Y	$E[g(X, Y)]$	FOR DISCRETE CASE $E[g(X, Y)] = \sum_y \sum_x g(x, y) p(x, y)$ FOR CONTINUOUS CASE $E[g(X, Y)] = \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} g(x, y) f(x, y) dx dy$
THE COVARIANCE OF X AND Y	$Cov(X, Y)$	IN GENERAL $Cov(X, Y) = E[(X - E[X])(Y - E[Y])]$ $= E[XY] - E[X]E[Y]$ $Var(X + Y) = Var[X] + Var[Y] + 2Cov[X, Y]$ $Var[X - Y] = Var[X] + Var[Y] - 2Cov[X, Y]$ If X and Y are independent then $Cov[X, Y] = 0$